

# The C Clustering Library

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The University of Tokyo, Institute of Medical Science, Human Genome Center

Michiel de Hoon, Seiya Imoto, Satoru Miyano

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The C Clustering Library for cDNA microarray data.

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This library was written at the Laboratory of DNA Information Analysis, Human Genome Center, Institute of Medical Science, University of Tokyo, 4-6-1 Shirokanedai, Minato-ku, Tokyo 108-8639, Japan.

Contact: [mdehoon@ims.u-tokyo.ac.jp](mailto:mdehoon@ims.u-tokyo.ac.jp)

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# 1 Introduction

Clustering is widely used in gene expression data analysis. By grouping genes together based on the similarity between their gene expression profiles, functionally related genes may be found. Such a grouping suggests the function of presently unknown genes.

The C Clustering Library is a collection of numerical routines that implement the clustering algorithms that are most commonly used. The routines can be applied both to genes and to arrays. The clustering algorithms are:

- Hierarchical clustering (pairwise centroid-, single-, complete-, and average-linkage);
- $k$ -means clustering;
- Self-Organizing Maps;
- Principal Component Analysis.

To measure the similarity or distance between gene expression data, eight distance measures are available:

- Pearson correlation;
- Absolute value of the Pearson correlation;
- Uncentered Pearson correlation (equivalent to the cosine of the angle between two data vectors);
- Absolute uncentered Pearson correlation (equivalent to the cosine of the smallest angle between two data vectors);
- Spearman's rank correlation;
- Kendall's  $\tau$ ;
- Euclidean distance;
- Harmonically summed Euclidean distance;
- City-block distance.

This library was written in ANSI C and can therefore be easily linked to other C/C++ programs. Cluster 3.0 (<http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>) is an example of such a program. This library may be particularly useful when called from a scripting language such as Python (<http://www.python.org>), Perl (<http://www.perl.org>), or Ruby (<http://www.ruby.org>). The C Clustering Library contains wrappers for Python and Perl; interfaces to other scripting languages may be generated using SWIG (<http://www.swig.org>).

This manual contains a description of clustering techniques, their implementation in the C Clustering Library, the Python and Perl modules that give access to the C Clustering Library, and information on how to use the routines in the library from other C or C++ programs.

The C Clustering Library was released under the Python License.

Michiel de Hoon ([mdehoon@ims.u-tokyo.ac.jp](mailto:mdehoon@ims.u-tokyo.ac.jp); [mdehoon@cal.berkeley.edu](mailto:mdehoon@cal.berkeley.edu)), Seiya Imoto, Satoru Miyano

Laboratory of DNA Information Analysis, Human Genome Center, Institute of Medical Science, University of Tokyo.

## 2 Distance functions

In order to cluster gene expression data into groups with similar genes or microarrays, we should first define what exactly we mean by *similar*. In the C Clustering Library, eight distance functions are available to measure similarity, or conversely, distance:

‘c’	Pearson correlation coefficient;
‘a’	Absolute value of the Pearson correlation coefficient;
‘u’	Uncentered Pearson correlation (equivalent to the cosine of the angle between two data vectors);
‘x’	Absolute uncentered Pearson correlation;
‘s’	Spearman’s rank correlation;
‘k’	Kendall’s $\tau$ ;
‘e’	Euclidean distance;
‘h’	Harmonically summed Euclidean distance;
‘b’	City-block distance.

The first six of these distance measures are related to the correlation coefficient, while the remaining three are related to the Euclidean distance. The characters in front of the distance measures are used as mnemonics to be passed to various routines in the C Clustering Library.

One of the properties one would like to see in a distance function is that it satisfies the triangle inequality:

$$d(\underline{u}, \underline{v}) \leq d(\underline{u}, \underline{w}) + d(\underline{w}, \underline{v}) \text{ for all } \underline{u}, \underline{v}, \underline{w}.$$

In everyday language, this equation means that the shortest distance between two points is a straight line.

Correlation-based distance functions usually define the distance  $d$  in terms of the correlation  $r$  as

$$d = 1 - r.$$

All correlation-based similarity measures are converted to a distance using this definition. Note that this distance function does not satisfy the triangle inequality. As an example, try

$$\underline{u} = (1, 0, -1);$$

$$\underline{v} = (1, 1, 0).$$

$$\underline{w} = (0, 1, 1);$$

Using the Pearson correlation, we find  $d(\underline{u}, \underline{w}) = 1.8660$  while  $d(\underline{u}, \underline{v}) + d(\underline{v}, \underline{w}) = 1.6340$ . None of the distance functions based on the correlation coefficient satisfy the triangle inequality; this is a general characteristic of the correlation coefficient. The Euclidean distance and the city-block distance, which are *metrics*, do satisfy the triangle inequality. The correlation-based distance functions are sometimes called *semi-metric*.

## 2.1 Data handling

The input to the distance functions contains two arrays and two row or column indices, instead of two data vectors. This makes it easier to calculate the distance between two columns in the gene expression data matrix. If the distance functions would require two vectors, we would have to extract two columns from the matrix and save them in two vectors to be passed to the distance function. In order to specify if the distance between rows or between columns is to be calculated, each distance function has a flag *transpose*. If *transpose*==0, then the distance between two rows is calculated. Otherwise, the distance between two columns is calculated.

## 2.2 Weighting

For most of the distance functions available in the C Clustering Library, a weight vector can be applied. The weight vector contains weights for the elements in the data vector. If the weight for element  $i$  is  $w_i$ , then that element is treated as if it occurred  $w_i$  times in the data. The weight do not have to be integers. For the Spearman rank correlation and Kendall's  $\tau$ , discussed below, the weights do not have a well-defined meaning and are therefore not implemented.

## 2.3 Missing Values

Often in microarray experiments, some of the data values are missing. In the distance functions, we therefore use an additional matrix *mask* which shows which data values are missing. If *mask*[i][j]==0, then *data*[i][j] is missing, and is not included in the distance calculation.

## 2.4 The Pearson correlation coefficient

The Pearson correlation coefficient is defined as

$$r = \frac{1}{n} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{\sigma_x} \right) \left( \frac{y_i - \bar{y}}{\sigma_y} \right)$$

in which  $\bar{x}, \bar{y}$  are the sample mean of  $x$  and  $y$  respectively, and  $\sigma_x, \sigma_y$  are the sample standard deviation of  $x$  and  $y$ . The Pearson correlation coefficient is a measure for how well a straight line can be fitted to a scatterplot of  $x$  and  $y$ . If all the points in the scatterplot lie on a straight line, the Pearson correlation coefficient is either +1 or -1, depending on whether the slope of line is positive or negative. If the Pearson correlation coefficient is equal to zero, there is no correlation between  $x$  and  $y$ .

The *Pearson distance* is then defined as

$$d_P \equiv 1 - r.$$

As the Pearson correlation coefficient lies between -1 and 1, the Pearson distance lies between 0 and 2.

Note that the Pearson correlation automatically centers the data by subtracting the mean, and normalizes them by dividing by the standard deviation. While such normalization may be useful in some situations (e.g., when clustering gene expression levels directly instead of gene expression ratios), information is being lost in this step. In particular, the magnitude of changes in gene expression is being ignored. This is in fact the reason that the Pearson distance does not satisfy the triangle inequality.

## 2.5 Absolute Pearson correlation

By taking the absolute value of the Pearson correlation, we find a number between zero and one. If the absolute value is one, all the points in the scatter plot lie on a straight line with either a positive or a negative slope. If the absolute value is equal to zero, there is no correlation between  $x$  and  $y$ .

The distance is defined as usual as

$$d_A \equiv 1 - |r|,$$

where  $r$  is the Pearson correlation coefficient. As the absolute value of the Pearson correlation coefficient lies between 0 and 1, the corresponding distance lies between 0 and 1 as well.

In the context of gene expression experiments, note that the absolute correlation is equal to one if the gene expression data of two genes/microarrays have a shape that is either exactly the same or exactly opposite. The absolute correlation coefficient should therefore be used with care.

## 2.6 Uncentered correlation (cosine of the angle)

In some cases, it may be preferable to use the *uncentered correlation* instead of the regular Pearson correlation coefficient. The uncentered correlation is defined as

$$r_U = \frac{1}{n} \sum_{i=1}^n \left( \frac{x_i}{\sigma_x^{(0)}} \right) \left( \frac{y_i}{\sigma_y^{(0)}} \right),$$

where

$$\sigma_x^{(0)} = \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2},$$

$$\sigma_y^{(0)} = \sqrt{\frac{1}{n} \sum_{i=1}^n y_i^2}.$$

This is the same expression as for the regular Pearson correlation coefficient, except that the sample means  $\bar{x}, \bar{y}$  are set equal to zero. The uncentered correlation may be appropriate if there is a zero reference state. For instance, in the case of gene expression data given in terms of log-ratios, a log-ratio equal to zero corresponds to the green and red signal being equal, which means that the experimental manipulation did not affect the gene expression.



The distance corresponding to the uncentered correlation coefficient is defined as

$$d_U \equiv 1 - r_U,$$

where  $r_U$  is the uncentered correlation. As the uncentered correlation coefficient lies between  $-1$  and  $1$ , the corresponding distance lies between  $0$  and  $2$ .

The uncentered correlation is equal to the cosine of the angle of the two data vectors in  $n$ -dimensional space, and is often referred to as such. (From this viewpoint, it would make more sense to define the distance as the arc cosine of the uncentered correlation coefficient).

## 2.7 Absolute uncentered correlation

As for the regular Pearson correlation, we can define a distance measure using the absolute value of the uncentered correlation:

$$d_{AU} \equiv 1 - |r_U|,$$

where  $r_U$  is the uncentered correlation coefficient. As the absolute value of the uncentered correlation coefficient lies between  $0$  and  $1$ , the corresponding distance lies between  $0$  and  $1$  as well.

Geometrically, the absolute value of the uncentered correlation is equal to the cosine between the supporting lines of the two data vectors (i.e., the angle without taking the direction of the vectors into consideration).

## 2.8 Spearman rank correlation

The Spearman rank correlation is an example of a non-parametric similarity measure. It is useful because it is more robust against outliers than the Pearson correlation.

To calculate the Spearman rank correlation, we replace each data value by their rank if we would order the data in each vector by their value. We then calculate the Pearson correlation between the two rank vectors instead of the data vectors.

Weights cannot be suitably applied to the data if the Spearman rank correlation is used, especially since the weights are not necessarily integers. The calculation of the Spearman rank correlation in the C Clustering Library therefore does not take any weights into consideration.

As in the case of the Pearson correlation, we can define a distance measure corresponding to the Spearman rank correlation as

$$d_S \equiv 1 - r_S,$$

where  $r_S$  is the Spearman rank correlation.

## 2.9 Kendall's $\tau$

Kendall's  $\tau$  is another example of a non-parametric similarity measure. It is similar to the Spearman rank correlation, but instead of the ranks themselves only the relative ranks are used to calculate  $\tau$ . As in the case of the Spearman rank correlation, the weights are ignored in the calculation.

We can define a distance measure corresponding to Kendall's  $\tau$  as

$$d_K \equiv 1 - \tau.$$

As Kendall's  $\tau$  is defined such that it will lie between  $-1$  and  $1$ , the corresponding distance will be between  $0$  and  $2$ .

## 2.10 Euclidean distance

The Euclidean distance is a true metric, as it satisfies the triangle inequality. The Euclidean distance is defined as

$$d = \sum_{i=1}^n (x_i - y_i)^2.$$

In this formula, the expression data  $x_i$  and  $y_i$  are subtracted directly from each other. We should therefore make sure that the expression data are properly normalized when using the Euclidean distance, for example by converting the measured gene expression levels to log-ratios.

Unlike the correlation-based distance functions, the Euclidean distance takes the magnitude of the expression data into account. It therefore preserves more information about the data and may be preferable. De Hoon, Imoto, Miyano (2002) give an example of the use of the Euclidean distance for  $k$ -means clustering.

## 2.11 Harmonically summed Euclidean distance

The harmonically summed Euclidean distance is a variation of the Euclidean distance, where the terms for the different dimensions are summed inversely (similar to the harmonic mean):

$$d = \left[ \frac{1}{n} \sum_{i=1}^n \left( \frac{1}{x_i - y_i} \right)^2 \right]^{-1}.$$

The harmonically summed Euclidean distance is more robust against outliers compared to the Euclidean distance. Note that the harmonically summed Euclidean distance is *not* a metric. For example, consider

$$\underline{u} = (1, 0);$$

$$\underline{v} = (0, 1);$$

$$\underline{w} = (1, 1).$$

This yields  $d(\underline{u}, \underline{v}) = 1$  while  $d(\underline{u}, \underline{w}) + d(\underline{w}, \underline{v}) = 0$ .

## 2.12 City-block distance

The city-block distance, alternatively known as the Manhattan distance, is related to the Euclidean distance. Whereas the Euclidean distance corresponds to the length of the shortest path between two points, the city-block distance is the sum of distances along each dimension:

$$d = \sum_{i=1}^n |x_i - y_i|.$$

This is equal to the distance you would have to walk between two points in a city, where you have to walk along city blocks. The city-block distance is a metric, as it satisfies the triangle inequality. As for the Euclidean distance, the expression data are subtracted directly from each other, and we should therefore make sure that they are properly normalized.

## 2.13 Calculating the distance between clusters

In the hierarchical clustering methods, the distance matrix between all genes/microarrays is first calculated, and at successive steps of the algorithm the new distance matrix is calculated from the previous distance matrix. In some cases, however, we would like to calculate the distance between clusters directly, given their members. For this purpose, the function `clusterdistance` can be used. This function can also be used to calculate the distance between two genes/microarrays by defining two clusters consisting of one gene/microarray each. While this function is not used internally in the C Clustering Library, it may be used by other C applications, and can also be called from Python (See Chapter 9 [Using the C Clustering Library with Python: Pycluster and Bio.Cluster], page 28) and Perl (See Chapter 10 [Using the C Clustering Library with Perl: Algorithm::Cluster], page 41).

The distance between two clusters can be defined in several ways. The distance between the arithmetic means of the two clusters is used in pairwise centroid-linkage clustering and in *k*-means clustering. For the latter, the distance between the medians of the two clusters can be used alternatively. The shortest pairwise distance between elements of the two clusters is used in pairwise single-linkage clustering, while the longest pairwise distance is used in pairwise maximum-linkage clustering. In pairwise average-linkage clustering, the distance between two clusters is defined as the average over the pairwise distances.

### Prototype

```
double clusterdistance (int nrows, int ncolums, double** data, int** mask,
double weight[], int n1, int n2, int index1[], int index2[], char dist, char
method, int transpose);
```

returns the distance between two clusters.

### Arguments

- `int nrows;`  
The number of rows in the *data* matrix, equal to the number of genes in the gene expression experiment.
- `int ncolums;`  
The number of columns in the *data* matrix, equal to the number of microarrays in the gene expression experiment.

- **double\*\* data;**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: `[nrows] [ncolumns]`.
- **int\*\* mask;**  
This array shows which elements in the *data* array, if any, are missing. If `mask[i] [j]==0`, then `data[i] [j]` is missing. Dimension: `[nrows] [ncolumns]`.
- **double weight[];**  
The weights that are used to calculate the distance. Dimension: `[ncolumns]` if *transpose*==0; `[nrows]` if *transpose*==1.
- **int n1;**  
The number of elements in the first cluster.
- **int n2;**  
The number of elements in the second cluster.
- **int index1[];**  
Contains the indices of the elements belonging to the first cluster. Dimension: `[n1]`.
- **int index2[];**  
Contains the indices of the elements belonging to the second cluster. Dimension: `[n2]`.
- **char dist;**  
Specifies which distance measure is used. See Chapter 2 [Distance functions], page 2.
- **char method;**  
Specifies how the distance between clusters is defined:
 

‘a’	Distance between the two cluster centroids (arithmetic mean);
‘m’	Distance between the two cluster centroids (median);
‘s’	Shortest pairwise distance between elements in the two clusters;
‘x’	Longest pairwise distance between elements in the two clusters;
‘v’	Average over the pairwise distances between elements in the two clusters.
- **int transpose;**  
If *transpose*==0, the distances between rows in the data matrix are calculated. Otherwise, the distances between columns are calculated.

### 3 Random number generator

The random number generator in the C Clustering Library is used to initialize the  $k$ -means clustering algorithm and Self-Organizing Maps (SOMs), as well as to randomly select a gene or microarray in the calculation of a SOM. We used the C version of the random number generator library `ranlib`, which is included in the source code distribution. It can also be downloaded from Netlib (<http://www.netlib.org/random/index.html>). This random number generator needs two seeds for initialization, for which we used the standard C random number generator `srand`. We initialize `srand` with the epoch time in seconds. The first two random numbers generated by `srand` are then used as seeds for the `ranlib` random number generator.

## 4 The distance matrix

The first step in clustering problems is usually to calculate the distance matrix. This matrix contains all the distances between the items that are being clustered. As the distance functions are symmetric, the distance matrix is also symmetric. Furthermore, the elements on the diagonal are zero, as the distance of an item to itself is zero. The distance matrix can therefore be stored as a ragged array, with the number of columns in each row equal to the (zero-offset) row number. The distance between items  $i$  and  $j$  is stored in location  $[i][j]$  if  $j < i$ , in  $[j][i]$  if  $j > i$ , while it is zero if  $j = i$ . Note that the first row of the distance matrix is empty. It is included for computational convenience, as including an empty row requires minimal storage.

### Prototype

```
double** distancematrix (int nrows, int ncolumns, double** data, int** mask,
double weight[], char dist, int transpose);
```

returns the distance matrix stored as a ragged array.

### Arguments

- **int nrows;**  
The number of rows in the data matrix, equal to the number of genes in the gene expression experiment.
- **int ncolumns;**  
The number of columns in the data matrix, equal to the number of microarrays in the gene expression experiment.
- **double\*\* data;**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension:  $[nrows][ncolumns]$ .
- **int\*\* mask;**  
This array shows which elements in the *data* array, if any, are missing. If  $mask[i][j]==0$ , then  $data[i][j]$  is missing. Dimension:  $[nrows][ncolumns]$ .
- **double weight[];**  
The weights that are used to calculate the distance. Dimension:  $[ncolumns]$  if *transpose*==0;  $[nrows]$  if *transpose*==1.
- **char dist;**  
Specifies which distance measure is used. See Chapter 2 [Distance functions], page 2.
- **int transpose;**  
If *transpose*==0, the distances between the rows in the data matrix are calculated. Otherwise, the distances between the columns are calculated.

## 5 Partitioning algorithms

Partitioning algorithms divide items into  $k$  clusters such that the sum of distances over the items to their cluster centers is minimal. The number of clusters  $k$  is specified by the user. In the C Clustering Library, three partitioning algorithms are available:

- $k$ -means clustering
- $k$ -medians clustering
- $k$ -medoids clustering

These algorithms differ in how the cluster center is defined. In  $k$ -means clustering, the cluster center is defined as the mean data vector averaged over all items in the cluster. Instead of the mean, in  $k$ -medians clustering the median is calculated for each dimension in the data vector. Finally, in  $k$ -medoids clustering the cluster center is defined as the item which has the smallest sum of distances to the other items in the cluster. This clustering algorithm is suitable for cases in which the distance matrix is known but the original data matrix is not available, for example when clustering proteins based on their structural similarity.

The expectation-maximization (EM) algorithm is commonly used to find the partitioning into  $k$  groups. The first step in the EM algorithm is to create  $k$  clusters and randomly assign items (genes or microarrays) to them. We then iterate:

- Calculate the centroid of each cluster;
- For each item, determine which cluster centroid is closest;
- Reassign the item to that cluster.

The iteration is stopped if no further item reassignments take place.

As the initial assignment of items to clusters is done randomly, usually a different clustering solution is found each time the EM algorithm is executed. To find the optimal clustering solution, the  $k$ -means algorithm is repeated many times, each time starting from a different initial random clustering. The sum of distances of the items to their cluster center is saved for each run, and the solution with the smallest value of this sum will be returned as the overall clustering solution.

How often the EM algorithm should be run depends on the number of items being clustered. As a rule of thumb, we can consider how often the optimal solution was found. This number is returned by the partitioning algorithms as implemented in this library. If the optimal solution was found many times, it is unlikely that better solutions exist than the one that was found. However, if the optimal solution was found only once, there may well be other solutions with a smaller within-cluster sum of distances.

### 5.1 Initialization

The  $k$ -means algorithm is initialized by randomly assigning items (genes or microarrays) to clusters. Special care should be taken to ensure that no empty clusters are produced. This is done by first choosing  $k$  items randomly and assigning each of them to a different cluster. The remaining items are then randomly assigned to clusters. Each cluster is thus guaranteed to contain at least one item.

## Prototype

```
void randomassign (int nclusters, int nelements, int clusterid[]);
```

## Arguments

- **int *nclusters***;  
The number of clusters.
- **int *nelements***;  
The number of elements (genes or microarrays) to be clustered.
- **int *clusterid*[]**;  
The cluster number to which each element was assigned. Space for this array should be allocated before calling `randomassign`. Dimension: [*nelements*].

## 5.2 Finding the cluster centroid

The centroid of a cluster can be defined in different ways. For  $k$ -means clustering, the centroid of a cluster is defined as the mean over all items in a cluster for each dimension separately. For robustness against outliers, in  $k$ -medians clustering the median is used instead of the mean. In  $k$ -medoids clustering, the cluster centroid is the item with the smallest sum of distances to the other items in the cluster. The C Clustering Library provides routines to calculate the cluster mean, the cluster median, and the cluster medoid.

### 5.2.1 Finding the cluster mean

The routine `getclustermean` calculates the centroids of the clusters by calculating the mean for each dimension separately over all items in a cluster. Missing data values are not included in the calculation of the mean. Whether the cluster means have a missing value is stored in an array *cmask*. If for cluster  $i$  the data values for dimension  $j$  are missing for all items, then *cmask*[ $i$ ][ $j$ ] (or *cmask*[ $j$ ][ $i$ ] if *transpose*==1) is set equal to zero. Otherwise, it is set equal to one.

## Prototype

```
void getclustermean (int nclusters, int nrows, int ncolumns, double** data, int**  
mask, int clusterid[], double** cdata, int** cmask, int transpose);
```

## Arguments

- **int *nclusters***;  
The number of clusters.
- **int *nrows***;  
The number of rows in the data matrix, equal to the number of genes in the gene expression experiment.
- **int *ncolumns***;  
The number of columns in the data matrix, equal to the number of microarrays in the gene expression experiment.



- **double\*\* data;**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: `[nrows][ncolumns]`.
- **int\*\* mask;**  
This array shows which elements in the *data* array, if any, are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. Dimension: `[nrows][ncolumns]`.
- **int clusterid[];**  
The cluster number to which each item belongs. Each element in this array should be between 0 and *nclusters*-1 inclusive. Dimension: `[nrows]` if *transpose*==0, or `[ncolumns]` if *transpose*==1.
- **double\*\* cdata;**  
This matrix stores the centroid information. Space for this matrix should be allocated before calling `getclustermean`. Dimension: `[nclusters][ncolumns]` if *transpose*==0 (row-wise clustering), or `[nrows][nclusters]` if *transpose*==1 (column-wise clustering).
- **int\*\* cmask;**  
This matrix stores which values in *cdata* are missing. If `cmask[i][j]==0`, then `cdata[i][j]` is missing. Space for *cmask* should be allocated before calling `getclustermean`. Dimension: `[nclusters][ncolumns]` if *transpose*==0 (row-wise clustering), or `[nrows][nclusters]` if *transpose*==1 (column-wise clustering).
- **int transpose;**  
This flag indicates whether row-wise (gene) or column-wise (microarray) clustering is being performed. If *transpose*==0, rows (genes) are being clustered. Otherwise, columns (microarrays) are being clustered.

### 5.2.2 Finding the cluster median

The routine `getclustermedian` calculates the centroids of the clusters by calculating the median for each dimension separately over all items in a cluster. Missing data values are not included in the calculation of the median. Whether the cluster medians have a missing value is stored in an array *cmask*. If for cluster *i* the data values for dimension *j* are missing for all items, then `cmask[i][j]` (or `cmask[j][i]` if *transpose*==1) is set equal to zero. Otherwise, it is set equal to one. Calculating the median may take significantly longer than calculating the mean.

#### Prototype

```
void getclustermedian (int nclusters, int nrows, int ncolumns, double** data,
int** mask, int clusterid[], double** cdata, int** cmask, int transpose);
```

#### Arguments

- **int nclusters;**  
The number of clusters.
- **int nrows;**  
The number of rows in the data matrix, equal to the number of genes in the gene expression experiment.

- **int *ncolumns*;**  
The number of columns in the data matrix, equal to the number of microarrays in the gene expression experiment.
- **double\*\* *data*;**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: [*nrows*] [*ncolumns*].
- **int\*\* *mask*;**  
This array shows which elements in the *data* array, if any, are missing. If *mask*[*i*][*j*]==0, then *data*[*i*][*j*] is missing. Dimension: [*nrows*] [*ncolumns*].
- **int *clusterid*[];**  
The cluster number to which each item belongs. Each element in this array should be between 0 and *nclusters*-1 inclusive. Dimension: [*nrows*] if *transpose*==0, or [*ncolumns*] if *transpose*==1.
- **double\*\* *cdata*;**  
This matrix stores the centroid information. Space for this matrix should be allocated before calling `getclustermedian`. Dimension: [*nclusters*] [*ncolumns*] if *transpose*==0 (row-wise clustering), or [*nrows*] [*nclusters*] if *transpose*==1 (column-wise clustering).
- **int\*\* *cmask*;**  
This matrix stores which values in *cdata* are missing. If *cmask*[*i*][*j*]==0, then *cdata*[*i*][*j*] is missing. Space for *cmask* should be allocated before calling `getclustermedian`. Dimension: [*nclusters*] [*ncolumns*] if *transpose*==0 (row-wise clustering), or [*nrows*] [*nclusters*] if *transpose*==1 (column-wise clustering).
- **int *transpose*;**  
This flag indicates whether row-wise (gene) or column-wise (microarray) clustering is being performed. If *transpose*==0, rows (genes) are being clustered. Otherwise, columns (microarrays) are being clustered.

### 5.2.3 Finding the cluster medoid

The cluster medoid is defined as the item which has the smallest sum of distances to the other items in the cluster. The `getclustermedoid` routine calculates the cluster centroids, given to which cluster each item belongs. The centroid is defined as the item with the smallest sum of distances to the other items.

#### Prototype

```
void getclustermedoid(int nclusters, int nelements, double** distance, int
clusterid[], int centroids[], double errors[]);
```

#### Arguments

- **int *nclusters*;**  
The number of clusters.
- **int *nelements*;**  
The total number of elements that are being clustered.

- **double\*\* *distmatrix*;**  
The distance matrix. The distance matrix is symmetric and has zeros on the diagonal. To save space, the distance matrix is stored as a ragged array. Dimension: [*nelements*] [] as a ragged array. The number of columns in each row is equal to the row number (starting from zero). Accordingly, the first row always has zero columns.
- **int *clusterid*[];**  
The cluster number to which each element belongs. Dimension: [*nelements*].
- **int *centroid*[];**  
For each cluster, the element of the item that was determined to be its centroid. Dimension: [*nclusters*].
- **int *errors*[];**  
For each cluster, the sum of distances between the items belonging to the cluster and the cluster centroid. Dimension: [*nclusters*].

### 5.3 The EM algorithm

The EM algorithm as implemented in the C Clustering Library first randomly assigns items to clusters using **randomassign**, followed by iterating to find a clustering solution with a smaller within-cluster sum of distances. During the iteration, first we find the centroids of all clusters, where the centroids are defined in terms of the mean, the median, or the medoid. The distances of each item to the cluster centers are calculated, and we determine for each item which cluster is closest. We then reassign the items to their closest clusters, and recalculate the cluster centers.

All items are first reassigned before recalculating the cluster centroids. This has two consequences:

- If unchecked, clusters may become empty if all their items are reassigned. For *k*-means and *k*-medians clustering, the EM routine therefore keeps track of the number of items in each cluster at all times, and prohibits an item to be reassigned to a different cluster if that would cause its current cluster to become empty. For *k*-medoids clustering, such a check is not needed, as the item that functions as the cluster centroid has a zero distance to itself, and would therefore not be reassigned to a different cluster anyway.
- In principle, the order in which items are reassigned to clusters does not matter. However, since we force an item to stay in a cluster if it is the last remaining item, for *k*-means and *k*-medians clustering we need to randomize the order anyway to ensure that not always the same items are forced to stay in a cluster. For *k*-medoids clustering, no such randomization is needed.

The EM algorithm terminates when no further reassignments take place. We noticed, however, that for some sets of initial cluster assignments, the EM algorithm fails to converge due to the same clustering solution reappearing periodically after a small number of iteration steps. In the EM algorithm as implemented in the C Clustering Library, the occurrence of such periodic solutions is checked for. After a given number of iteration steps, the current clustering result is saved as a reference. By comparing the clustering result after each subsequent iteration step to the reference state, we can determine if a previously encountered clustering result is found. In such a case, the iteration is halted. If after a given number of iterations the reference state has not yet been encountered, the current

clustering solution is saved to be used as the new reference state. Initially, ten iteration steps are executed before resaving the reference state. This number of iteration steps is doubled each time, to ensure that periodic behavior with longer periods can also be detected.

## 5.4 Finding the optimal solution

### 5.4.1 *k*-means and *k*-medians

The optimal solution is found by executing the EM algorithm repeatedly and saving the best clustering solution that was returned by it. This can be done automatically by calling the routine `kcluster`. This procedure first initializes `ranlib`'s random number generator. The routine to calculate the cluster centroid and the distance function are selected based on the arguments passed to `kcluster`.

The EM algorithm is then executed repeatedly, saving the best clustering solution that was returned by these routines. In addition, `kcluster` counts how often the EM algorithm found this solution. If it was found many times, we can assume that there are no other solutions possible with a smaller within-cluster sum of distances. If, however, the solution was found only once, it may well be that better clustering solutions exist.

### Prototype

```
void kcluster (int nclusters, int nrows, int ncolumns, double** data, int** mask,
double weight[], int transpose, int npass, char method, char dist, int clusterid[],
double** cdata, double* error, int* ifound);
```

### Arguments

- `int nclusters;`  
The number of clusters *k*.
- `int nrows;`  
The number of rows in the data matrix, equal to the number of genes in the gene expression experiment.
- `int ncolumns;`  
The number of columns in the data matrix, equal to the number of microarrays in the gene expression experiment.
- `double** data;`  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: `[nrows][ncolumns]`.
- `int** mask;`  
This array shows which elements in the `data` array, if any, are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. Dimension: `[nrows][ncolumns]`.
- `double weight[];`  
The weights that are used to calculate the distance. Dimension: `[ncolumns]` if `transpose==0`; `[nrows]` if `transpose==1`.

- **int transpose;**  
This flag indicates whether row-wise (gene) or column-wise (microarray) clustering is being performed. If *transpose==0*, rows (genes) are being clustered. Otherwise, columns (microarrays) are being clustered.
- **int npass;**  
The number of times the EM algorithm should be run. If *npass > 0*, each run of the EM algorithm uses a different (random) initial clustering. If *npass == 0*, then the EM algorithm is run with an initial clustering specified by *clusterid*. For *npass > 0*, items are reassigned to clusters in a randomized order. Since the cluster centroids are recalculated only once after all items have been considered for reassignment, the order of item reassignment is relevant only when the last item in a cluster is about to be reassigned to a different cluster. To prevent clusters from becoming empty, such reassignments are not allowed; which items are reassigned may therefore depend on the order in which items are considered. For *npass==0*, the EM algorithm is run only once, without randomizing the order in which items are reassigned to clusters, using the initial clustering as specified by *clusterid*. The order in which items are reassigned is identical to the order in which items are given in the data matrix.
- **char method;**  
Specifies whether the arithmetic mean (*method=='a'*) or the median (*method=='m'*) should be used to calculate the cluster center.
- **char dist;**  
Specifies which distance function should be used. The character should correspond to one of the distance functions that are available in the C Clustering Library. See Chapter 2 [Distance functions], page 2.
- **int clusterid[];**  
This array will be used to store the cluster number to which each item was assigned by the clustering algorithm. Space for *clusterid* should be allocated before calling *kcluster*. If *npass==0*, then the contents of *clusterid* on input is used as the initial assignment of items to clusters; on output, *clusterid* contains the optimal clustering solution found by the EM algorithm. Dimension: [*nrows*] if *transpose==0*, or [*ncolumns*] if *transpose==1*.
- **double\*\* cdata;**  
This matrix stores the centroid information. Space for *cdata* should be allocated before calling *kcluster*. Dimension: [*nclusters*][*ncolumns*] if *transpose==0* (row-wise clustering), or [*nrows*][*nclusters*] if *transpose==1* (column-wise clustering).
- **double\* error;**  
The sum of distances of the items to their cluster center after *k*-means clustering, which can be used as a criterion to compare clustering solutions produced in different calls to *kcluster*.
- **int\* ifound;**  
Returns how often the optimal clustering solution was found.

### 5.4.2 *k*-medoids

The *kmedoids* routine performs *k*-medoids clustering on a given set of elements, using the distance matrix and the number of clusters passed by the user. Multiple passes are being

made to find the optimal clustering solution, each time starting from a different initial clustering.

## Prototype

### Arguments

- **int *nclusters*;**  
The number of clusters to be found.
- **int *nelements*;**  
The number of elements to be clustered.
- **double\*\* *distmatrix*;**  
The distance matrix. The distance matrix is symmetric and has zeros on the diagonal. To save space, the distance matrix is stored as a ragged array. Dimension: [*nelements*] [] as a ragged array. The number of columns in each row is equal to the row number (starting from zero). Accordingly, the first row always has zero columns.
- **int *npass*;**  
The number of times the EM algorithm should be run. If *npass* > 0, each run of the EM algorithm uses a different (random) initial clustering. If *npass* == 0, then the EM algorithm is run with an initial clustering specified by *clusterid*. The order in which items are reassigned is identical to the order in which items are given in the distance matrix.
- **int *clusterid*[];**  
This array will be used to store the cluster number to which each item was assigned by the clustering algorithm. Space for *clusterid* should be allocated before calling *kcluster*. On input, if *npass*==0, then *clusterid* contains the initial clustering assignment from which the clustering algorithm starts; all numbers in *clusterid* should be between 0 and *nelements*-1 inclusive. If *npass*!=0, *clusterid* is ignored on input. On output, *clusterid* contains the number of the cluster to which each item was assigned in the optimal clustering solution. On output, the number of a cluster is defined as the item number of the centroid of the cluster. Dimension: [*nelements*].
- **double\* *error*;**  
The sum of distances of the items to their cluster center after *k*-means clustering, which can be used as a criterion to compare clustering solutions produced in different calls to *kmedoids*.
- **int\* *ifound*;**  
Returns how often the optimal clustering solution was found.

## 6 Hierarchical clustering

### 6.1 Hierarchical clustering methods

Hierarchical clustering methods are inherently different from the  $k$ -means clustering method. In hierarchical clustering methods, gene expression data are described in terms of a tree structure. While the existence of such a tree structure may be debatable, the hierarchical clustering methods are quite popular in the analysis of gene expression data.

The first step in hierarchical clustering is to calculate the distance matrix, specifying all the distances between the items to be clustered. Next, we create a node by joining the two closest items. Subsequent nodes are created by pairwise joining of items or nodes based on the distance between them, until all items belong to the same node. A tree structure can then be created by retracing which items and nodes were merged. Unlike the EM algorithm, which is used in  $k$ -means clustering, the complete process of hierarchical clustering is deterministic.

Several flavors of hierarchical clustering exist, which differ in how the distance between subnodes is defined in terms of their members. In the C Clustering Library, pairwise single, maximum, average, and centroid linkage are available.

- In pairwise single-linkage clustering, the distance between two nodes is defined as the shortest distance among the pairwise distances between the members of the two nodes.
- In pairwise maximum-linkage clustering, alternatively known as pairwise complete-linkage clustering, the distance between two nodes is defined as the longest distance among the pairwise distances between the members of the two nodes.
- In pairwise average-linkage clustering, the distance between two nodes is defined as the average over all pairwise distances between the elements of the two nodes.
- In pairwise centroid-linkage clustering, the distance between two nodes is defined as the distance between their centroids. The centroids are calculated by taking the mean over all the elements in a cluster. As the distance from each newly formed node to existing nodes and items need to be calculated at each step, the computing time of pairwise centroid-linkage clustering may be significantly longer than for the other hierarchical clustering methods. Pairwise centroid-linkage clustering is sometimes referred to as pairwise average-linkage clustering.

For pairwise single-, complete-, and average-linkage clustering, the distance between two nodes can be found directly from the distances between the individual items. Therefore, the clustering algorithm does not need access to the original gene expression data, once the distance matrix is known. For pairwise centroid-linkage clustering, however, the centroids of newly formed subnodes can only be calculated from the original data and not from the distance matrix.

The `treecluster` routine described below implements pairwise single-, complete, average-, and centroid-linkage clustering. A pointer *distmatrix* to the distance matrix can be passed as one of the arguments to `treecluster`; if this pointer is `NULL`, the `treecluster` routine will calculate the distance matrix from the gene expression data using the arguments *data*, *mask*, *weight*, and *dist*. For pairwise single-, complete-, and average-linkage clustering, the `treecluster` routine ignores these four arguments

if *distmatrix* is given, as the distance matrix by itself is sufficient for the clustering calculation. For pairwise centroid-linkage clustering, the arguments *data*, *mask*, *weight*, and *dist* are always needed, even if *distmatrix* is available.

The **treecluster** routine will complete faster if it can make use of a previously calculated distance matrix passed as the *distmatrix* argument. Note, however, that newly calculated distances are stored in the distance matrix, and its elements may be rearranged during the clustering calculation. Therefore, in order to save the original distance matrix, it should be copied before **treecluster** is called. The memory that was allocated by the calling routine for the distance matrix will not be deallocated by **treecluster**, and should be deallocated by the calling routine after **treecluster** returns. If *distmatrix* is NULL, however, **treecluster** takes care both of the allocation and the deallocation of memory for the distance matrix.

## Prototype

```
void treecluster (int nrows, int ncolumns, double** data, int** mask, double
weight[], int applyscale, int transpose, char dist, char method, int result[][2],
double linkdist[], double** distmatrix);
```

## Arguments

- **int nrows;**  
The number of rows in the *data* matrix, equal to the number of genes in the gene expression experiment.
- **int ncolumns;**  
The number of columns in the *data* matrix, equal to the number of microarrays in the gene expression experiment.
- **double\*\* data;**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: [*nrows*] [*ncolumns*].
- **int\*\* mask;**  
This array shows which elements in the *data* array, if any, are missing. If *mask*[*i*][*j*]==0, then *data*[*i*][*j*] is missing. Dimension: [*nrows*] [*ncolumns*].
- **double weight[];**  
The weights that are used to calculate the distance. Dimension: [*ncolumns*] if *transpose*==0; [*nrows*] if *transpose*==1.
- **int applyscale;**  
If *applyscale* is nonzero, then the distances in *linkdist* are scaled such that all distances are between zero and two, as in case of the Pearson distance. Otherwise, no scaling is applied.
- **int transpose;**  
This flag indicates whether row-wise (gene) or column-wise (microarray) clustering is being performed. If *transpose*==0, rows (genes) are being clustered. Otherwise, columns (microarrays) are being clustered.
- **char dist;**  
Specifies which distance measure is used. See Chapter 2 [Distance functions], page 2.



- **char method;**  
Specifies which type of hierarchical clustering is used:  
's': pairwise single-linkage clustering  
'm': pairwise maximum- (or complete-) linkage clustering  
'a': pairwise average-linkage clustering  
'c': pairwise centroid-linkage clustering
- **int result[][2];**  
The clustering solution. Each row in the matrix describes one linking event. The two columns contain the numbers of the nodes that were joined. The original elements are numbered {0, ..., *nelements*-1}, nodes are numbered {-1, ..., -(*nelements*-1)}. Note that the number of nodes is one less than the number of elements. Space for this array should be allocated before calling **treecluster**. Dimension: [*nrows*-1][2] if *transpose*==0; [*ncolumns*-1][2] if *transpose*==1.
- **double linkdist[];**  
For each node, the distance between the two subnodes that were joined. Dimension: [*nrows*-1] if *transpose*==0; [*ncolumns*-1] if *transpose*==1.
- **double\*\* distmatrix;**  
The distance matrix, stored as a ragged array. This argument is optional; if the distance matrix is not available, it can be passed as NULL. In that case, **treecluster** will allocate memory space for the distance matrix, calculate it from the gene expression data, and deallocate the memory space before returning. If the distance matrix happens to be available, the hierarchical clustering calculation can be completed faster by passing it as the *distmatrix* argument. Note that the contents of the distance matrix will be modified by the clustering algorithm in **treecluster**. The memory that was allocated for the distance matrix should be deallocated by the calling routine after **treecluster** returns. Dimension: Ragged array, [*nrows*][] if *transpose*==0, or [*ncolumns*][] if *transpose*==1. In both cases, the number of columns in each row is equal to the row number (starting from zero). Accordingly, the first row always has zero columns.

## 6.2 Cutting a hierarchical clustering tree

The tree structure generated by the hierarchical clustering routine **treecluster** can be further analyzed by dividing the genes or microarrays into *n* clusters, where *n* is some positive integer less than or equal to the number of elements that were clustered. This can be achieved by ignoring the top *n* - 1 linking events in the tree structure, resulting in *n* separated subnodes. The elements in each subnode are then assigned to the same cluster. The routine **cuttree** determines to which cluster each element is assigned, based on the hierarchical clustering result stored in the tree structure.

### Prototype

```
void cuttree (int nelements, int tree[][2], int nclusters, int clusterid[]);
```

### Arguments

- **int *nelements*;**

The number of elements whose clustering results are stored in the *tree* hierarchical clustering result.

- `int tree[][2];`  
The hierarchical clustering solution. Each row in the matrix describes one linking event. The two columns contain the numbers of the nodes that were joined. The original elements are numbered  $\{0, \dots, nelements-1\}$ , nodes are numbered  $\{-1, \dots, -(nelements-1)\}$ . Note that the number of nodes is one less than the number of elements. The `cuttree` routine performs some error checking of the structure of the *tree* argument in order to avoid segmentation faults. However, errors in the structure of *tree* that would not result in segmentation faults will in general not be detected. Dimension:  $[nelements-1][2]$ .
- `int nclusters;`  
The desired number of clusters. The number of clusters should be positive, and less than or equal to *nelements*.
- `int clusterid[];`  
The cluster number to which each element is assigned. Memory space for *clusterid* should be allocated before `cuttree` is called. Dimension:  $[nelements]$ .

## 7 Self-Organizing Maps

Self-Organizing Maps (SOMs) were invented by Kohonen to describe neural networks (see for instance Kohonen, 1997). Tamayo (1999) first applied Self-Organizing Maps to gene expression data.

SOMs organize items into clusters that are situated in some topology. Usually a rectangular topology is chosen. The clusters generated by SOMs are such that neighboring clusters in the topology are more similar to each other than clusters far from each other in the topology.

The first step to calculate a SOM is to randomly assign a data vector to each cluster in the topology. If genes are being clustered, then the number of elements in each data vector is equal to the number of microarrays in the experiment.

An SOM is then generated by taking genes one at a time, and finding which cluster in the topology has the closest data vector. The data vector of that cluster, as well as those of the neighboring clusters, are adjusted using the data vector of the gene under consideration. The adjustment is given by

$$\Delta \underline{x}_{\text{cell}} = \tau \cdot (\underline{x}_{\text{gene}} - \underline{x}_{\text{cell}}).$$

The parameter  $\tau$  is a parameter that decreases at each iteration step. We have used a simple linear function of the iteration step:

$$\tau = \tau_{\text{init}} \cdot \left(1 - \frac{i}{n}\right),$$

in which  $\tau_{\text{init}}$  is the initial value of  $\tau$  as specified by the user,  $i$  is the number of the current iteration step, and  $n$  is the total number of iteration steps to be performed. While changes are made rapidly in the beginning of the iteration, at the end of iteration only small changes are made.

All clusters within a radius  $R$  are adjusted to the gene under consideration. This radius decreases as the calculation progresses as

$$R = R_{\text{max}} \cdot \left(1 - \frac{i}{n}\right),$$

in which the maximum radius is defined as

$$R_{\text{max}} = \sqrt{N_x^2 + N_y^2},$$

where  $(N_x, N_y)$  are the dimensions of the rectangle defining the topology.

The routine `somcluster` carries out the complete SOM algorithm. First it initializes the random number generator. The distance function to be used is specified by `dist`. The node data are then initialized using the `ranlib` random number generator. The order in which genes or microarrays are used to modify the SOM is also randomized. The total number of iterations is specified by `niter`, given by the user.

### Prototype

```
void somcluster (int nrows, int ncolumns, double** data, int** mask, double
weight[], int transpose, int nxgrid, int nygrid, double inittau, int niter, char dist,
double*** celldata, int clusterid[][2]);
```

## Arguments

- **int *nrows***;  
The number of rows in the data matrix, equal to the number of genes in the gene expression experiment.
- **int *ncolumns***;  
The number of columns in the data matrix, equal to the number of microarrays in the gene expression experiment.
- **double\*\* *data***;  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise. Dimension: [*nrows*] [*ncolumns*].
- **int\*\* *mask***;  
This array shows which elements in the *data* array, if any, are missing. If *mask*[*i*][*j*]==0, then *data*[*i*][*j*] is missing. Dimension: [*nrows*] [*ncolumns*].
- **double *weight*[]**;  
The weights that are used to calculate the distance. Dimension: [*ncolumns*] if *transpose*==0; [*nrows*] if *transpose*==1.
- **int *transpose***;  
This flag indicates whether row-wise (gene) or column-wise (microarray) clustering is being performed. If *transpose*==0, rows (genes) are being clustered. Otherwise, columns (microarrays) are being clustered.
- **int *nxgrid***;  
The number of cells horizontally in the rectangular topology containing the clusters.
- **int *nygrid***;  
The number of cells vertically in the rectangular topology containing the clusters.
- **double *inittau***;  
The initial value for the parameter  $\tau$  that is used in the SOM algorithm. A typical value for *inittau* is 0.02, which was used in Michael Eisen's Cluster/TreeView program.
- **int *niter***;  
The total number of iterations.
- **char *dist***;  
Specifies which distance measure is used. See Chapter 2 [Distance functions], page 2.
- **double\*\*\* *celldata***;  
The data vectors of the clusters in the rectangular topology that were found by the SOM algorithm. These correspond to the cluster centroids. The first dimension is the horizontal position of the cluster in the rectangle, the second dimension is the vertical position of the cluster in the rectangle, while the third dimension is the dimension along the data vector. The **somcluster** routine does not allocate storage space for the *celldata* array. Space should be allocated before calling **somcluster**. Alternatively, if *celldata* is equal to NULL, the **somcluster** routine allocates space for *celldata* and frees it before returning. In that case, **somcluster** does not return the data vectors of the clusters that were found. Dimension: [*nxgrid*] [*nygrid*] [*ncolumns*] if *transpose*==0, or [*nxgrid*] [*nygrid*] [*nrows*] if *transpose*==1.
- **int *clusterid*[][2]**;  
Specifies the cluster to which a gene or microarray was assigned, using two integers

to identify the horizontal and vertical position of a cell in the grid for each gene or microarray. Gene or microarrays are assigned to clusters in the rectangular grid by determining which cluster in the rectangular topology has the closest data vector. Space for the *clusterid* argument should be allocated before calling **somcluster**. If *clusterid* is NULL, the **somcluster** routine ignores this argument and does not return the cluster assignments. Dimension: [*nrows*][2] if *transpose*==0; [*ncolumns*][2] if *transpose*==1.

## 8 Principal Component Analysis

Principal Component Analysis (PCA) is a widely used technique for analyzing multivariate data. In PCA, the data vectors are written as a linear sum over principal components. The number of principal components is equal to the number of dimensions of the data vectors.

The principal components are chosen such that they maximally explain the variance in the data vectors. For example, in case of 3D data vectors, the data can be represented as an ellipsoidal cloud of points in three dimensional space. The first principal component would be the longest axis of the ellipsoid, the second principal component would be the second longest axis of the ellipsoid, and the third principal component would be the shortest axis. In other words, the principal components are ordered by the amount of variance they explain.

Each data point can be reconstructed by a suitable linear combination of the principal components. However, in order to reduce the dimensionality of the data, usually only the most important principal components are used. The remaining variance present in the data is then regarded as unexplained variance.

The principal components can be found by calculating the eigenvectors of the covariance matrix of the data. The corresponding eigenvalues determine how much of the variance present in the data is explained by each principal component.

The eigenvectors are found by calculating the singular value decomposition of the data matrix. For this purpose, we have included a routine to calculate the singular value decomposition of a matrix. This subroutine is a translation in C of the Algol procedure `svd` (Golub and Reinsch, 1970). Python users can use the `singular_value_decomposition` routine instead, which is part of the `LinearAlgebra` package of Numerical Python.

A practical example of applying Principal Component Analysis to gene expression data is presented by Yeung and Ruzzo (2001).

### Prototype

```
void svd (int nrows, int ncolums, double** U, double S[], double** V, int*
ierror);
```

calculates the singular value decomposition  $U_{\text{input}} = U_{\text{output}} \cdot S \cdot V^T$ . Householder bidiagonalization and a variant of the QR algorithm are used.

### Arguments

- `int nrows`  
The number of rows in  $U$ . The number of rows should be greater than or equal to the number of columns.
- `int ncolums`  
The number of columns in  $U$  and the order of  $V$ .
- `double** U`;  
On input:  $U$  is the rectangular matrix to be decomposed. On output: The contents of  $U$  is replaced such that  $U_{\text{input}} = U_{\text{output}} \cdot S \cdot V^T$ . Dimension:  $[nrows][ncolums]$ .
- `double* S`;  
The  $ncolums$  non-negative singular values of the matrix  $U$ , unordered. If an error

exit is made, the singular values should be correct for indices { *\*ierror*, *\*ierror*+1, . . . , *ncolumns*-1}. Dimension: [*ncolumns*].

- **double\*\*** *V*;

The orthogonal matrix *V* of the decomposition. If an error exit is made, the columns of *V* corresponding to indices of correct singular values should be correct. Dimension: [*ncolumns*] [*ncolumns*].

- **int\*** *ierror*;

Error exit: *\*ierror*==0 for normal return, and *\*ierror*==*k* if the *k*<sup>th</sup> singular value has not been determined after 30 iterations.

## 9 Using the C Clustering Library with Python: Pycluster and Bio.Cluster

The C Clustering Library is particularly useful when used as a module to a scripting language. We used `pyfort` (<http://pyfortran.sourceforge.net>) to generate an interface of some of the routines in the C Clustering Library to the scripting language Python (<http://www.python.org>). This chapter describes the routines in the C Clustering Library as seen from Python.

To make the routines available to Python, install Pycluster (see Section 11.1 [Installing the C Clustering Library for Python], page 50). From Python, then type

```
from Pycluster import *
```

Pycluster is also available as part of Biopython (<http://www.biopython.org>), in which case you should use

```
from Bio.Cluster import *
```

This will give you access to the following Python functions:

- `kcluster`;
- `kmedoids`;
- `treecluster`;
- `cuttree`;
- `somcluster`;
- `clustercentroid`;
- `clusterdistance`;
- `readdatafile`;
- `writeclusterfiles`.

### 9.1 Partitioning algorithms

#### 9.1.1 *k*-means and *k*-medians clustering: `kcluster`

`clusterid, centroids, error, nfound = kcluster (data, nclusters=2, mask=None, weight=None, transpose=0, npass=1, method='a', dist='e', initialid=None)` implements the *k*-means and *k*-medians clustering algorithms.

#### Arguments

- **data**  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **nclusters**  
The number of clusters *k*.
- **mask**  
Array of integers showing which data are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. If `mask==None`, then there are no missing data.
- **weight**  
contains the weights to be used when calculating distances. If `weight==None`, then equal weights are assumed.



- **transpose**  
Determines if genes or microarrays are being clustered. If **transpose==0**, genes (rows) are being clustered. If **transpose==1**, microarrays (columns) are clustered.
- **npass**  
The number of times the *k*-means clustering algorithm is performed, each time with a different (random) initial condition. If **initialid** is given, the value of *npass* is ignored, as the clustering algorithm behaves deterministically in that case.
- **method**  
describes how the center of a cluster is found:
  - method=='a'**: arithmetic mean;
  - method=='m'**: median.

For other values of **method**, the arithmetic mean is used.
- **dist**  
defines the distance function to be used:
  - dist=='c'**: correlation;
  - dist=='a'**: absolute value of the correlation;
  - dist=='u'**: uncentered correlation;
  - dist=='x'**: absolute uncentered correlation;
  - dist=='s'**: Spearman's rank correlation;
  - dist=='k'**: Kendall's  $\tau$ ;
  - dist=='e'**: Euclidean distance;
  - dist=='h'**: Harmonically summed Euclidean distance;
  - dist=='b'**: City-block distance.

For other values of **dist**, the default (Euclidean distance) is used.
- **initialid**  
Specifies the initial clustering to be used for the EM algorithm. If **initialid==None**, then a different random initial clustering is used for each of the **npass** runs of the EM algorithm. If **initialid** is not **None**, then it should be equal to a 1D array containing the cluster number (between 0 and **nclusters-1**) for each item. Each cluster should contain at least one item. With the initial clustering specified, the EM algorithm is deterministic.

## Return values

This function returns a tuple (*clusterid*, *centroids*, *error*, *nfound*).

- *clusterid*  
An array containing the number of the cluster to which each gene/microarray was assigned.
- *centroids*  
An array containing the gene expression data for the cluster centers, with dimensions (*number of clusters, number of microarrays*) if genes were clustered, or (*number of genes, number of clusters*) if microarrays were clustered.

- *error*  
The within-cluster sum of distances for the optimal clustering solution.
- *nfound*  
The number of times the optimal solution was found.

### 9.1.2 *k*-medoids clustering: `kmedoids`

`clusterid, error, nfound = kmedoids (distance, nclusters=2, npass=1, initialid=None)`  
implements the *k*-medoids clustering algorithm.

#### Arguments

- **distance**  
An array containing the distance matrix between the elements. You can either pass a 2D Numerical Python array (in which only the left-lower part of the array will be accessed), or you can pass a 1D Numerical Python array containing consecutively the distances in the left-lower part of the distance matrix. Examples are:  

```
distance = array([[0.0, 1.1, 2.3], [1.1, 0.0, 4.5], [2.3, 4.5, 0.0]])
```

and  

```
distance = array([1.1, 2.3, 4.5])
```

These two expressions correspond to the same distance matrix.
- **nclusters**  
The number of clusters *k*.
- **npass**  
The number of times the *k*-means clustering algorithm is performed, each time with a different (random) initial condition. If **initialid** is given, the value of **npass** is ignored, as the clustering algorithm behaves deterministically in that case.
- **initialid**  
Specifies the initial clustering to be used for the EM algorithm. If **initialid==None**, then a different random initial clustering is used for each of the **npass** runs of the EM algorithm. If **initialid** is not **None**, then it should be equal to a 1D array containing the cluster number (between 0 and **nclusters-1**) for each item. Each cluster should contain at least one item. With the initial clustering specified, the EM algorithm is deterministic.

#### Return values

This function returns a tuple (*clusterid*, *error*, *nfound*).

- *clusterid*  
An array containing the number of the cluster to which each item was assigned, where the cluster number is defined as the item number of the item representing the cluster centroid.
- *error*  
The within-cluster sum of distances for the optimal *k*-medoids clustering solution.
- *nfound*  
The number of times the optimal solution was found.

## 9.2 Hierarchical clustering

The pairwise single-, maximum-, average-, and centroid-linkage clustering methods are accessible through the function `treecluster`. The hierarchical clustering routines can be applied either on the original gene expression data, or (except for centroid-linkage clustering) on the distance matrix directly. The tree structure generated by `treecluster` can be cut in order to separate the elements into a given number of clusters.

### 9.2.1 Hierarchical clustering methods: `treecluster`

`tree, linkdist = treecluster(data=None, mask=None, weight=None, applyscale=0, transpose=0, dist='e', method='m', distancematrix=None)`  
implements the hierarchical clustering methods.

#### Arguments

- **data**  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise. Either **data** or **distancematrix** should be `None`.
- **mask**  
Array of integers showing which data are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. If `mask==None`, then there are no missing data.
- **weight**  
contains the weights to be used when calculating distances. If `weight==None`, then equal weights are assumed.
- **applyscale**  
If **applyscale** is nonzero, then the distances in `linkdist` are scaled such that all distances are between zero and two, as in case of the Pearson distance. Otherwise, no scaling is applied.
- **transpose**  
Determines if genes or microarrays are being clustered. If `transpose==0`, genes (rows) are being clustered. If `transpose==1`, microarrays (columns) are clustered.
- **dist**  
defines the distance function to be used:
  - `dist=='c'`: correlation;
  - `dist=='a'`: absolute value of the correlation;
  - `dist=='u'`: uncentered correlation;
  - `dist=='x'`: absolute uncentered correlation;
  - `dist=='s'`: Spearman's rank correlation;
  - `dist=='k'`: Kendall's  $\tau$ ;
  - `dist=='e'`: Euclidean distance;
  - `dist=='h'`: Harmonically summed Euclidean distance;
  - `dist=='b'`: City-block distance.
- **method**  
defines the linkage method to be used:

`method=='s':` pairwise single-linkage clustering  
`method=='m':` pairwise maximum- (or complete-) linkage clustering  
`method=='c':` pairwise centroid-linkage clustering  
`method=='a':` pairwise average-linkage clustering

- **distancematrix**

The distance matrix, which should be square and symmetric. Either **data** or **distancematrix** should be **None**. If **data** is **None** and **distancematrix** is given, the arguments **mask**, **weights**, **transpose**, and **dist** are ignored. Note that pairwise single-, maximum-, and average-linkage clustering can be calculated from the distance matrix, but pairwise centroid-linkage cannot. For pairwise centroid-linkage clustering, the argument **data** should be given instead of **distancematrix**.

## Return values

This function returns a tuple (*tree*, *linkdist*).

- **tree**

An array with dimensions (*number of items* - 1, 2), where the number of items is the number of genes if genes were clustered, or the number of microarrays if microarrays were clustered. Each row in the array describes a pairwise linking event, where the two columns each contain the number of one gene/microarray or cluster. Genes/microarrays are numbered from 0 to (*number of items* - 1), while clusters are numbered -1 to -(*number of items*-1).

- **linkdist**

A 1D array with (*number of items* - 1) elements, representing the distance between the two subnodes for each node.

### 9.2.2 Cutting a hierarchical clustering tree: **cuttree**

`clusterid = cuttree(tree, nclusters=1)`

groups the elements into *nclusters* clusters based on the tree structure generated by the hierarchical clustering routine **treecluster**.

## Arguments

- **tree**

The array **tree** contains the hierarchical clustering result generated by **treecluster**. Each row in the array describes a pairwise linking event, where the two columns each contain the number of one element or cluster. Elements are numbered from 0 to (*number of elements* - 1), while clusters are numbered -1 to -(*number of elements*-1).

- **nclusters**

The desired number of clusters; **nclusters** should be positive, and less than or equal to the number of elements.

## Return values

This function returns the array *clusterid*.

- *clusterid*

An array containing the number of the cluster to which each gene/microarray is assigned.

### 9.3 Self-Organizing Maps: somcluster

*clusterid*, *celldata* = somcluster(data, mask=None, weight=None, transpose=0, nxgrid=2, nygrid=1, inittau=0.02, niter=1, dist='e')

implements a Self-Organizing Map on a rectangular grid.

#### Arguments

- **data**  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
Array of integers showing which data are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. If `mask==None`, then there are no missing data.
- **weight**  
contains the weights to be used when calculating distances. If `weight==None`, then equal weights are assumed.
- **transpose**  
Determines if genes or microarrays are being clustered. If `transpose==0`, genes (rows) are being clustered. If `transpose==1`, microarrays (columns) are clustered.
- **nxgrid, nygrid**  
The number of cells horizontally and vertically in the rectangular grid, on which the Self-Organizing Map is calculated.
- **inittau**  
The initial value for the parameter  $\tau$  that is used in the SOM algorithm. A default value for `inittau` is 0.02, which was used in Michael Eisen's Cluster/TreeView program.
- **niter**  
The number of iterations to be performed.
- **dist**  
defines the distance function to be used:
  - `dist=='c'`: correlation;
  - `dist=='a'`: absolute value of the correlation;
  - `dist=='u'`: uncentered correlation;
  - `dist=='x'`: absolute uncentered correlation;
  - `dist=='s'`: Spearman's rank correlation;
  - `dist=='k'`: Kendall's  $\tau$ ;
  - `dist=='e'`: Euclidean distance;
  - `dist=='h'`: Harmonically summed Euclidean distance;
  - `dist=='b'`: City-block distance.

## Return values

This function returns the tuple (*clusterid*, *celldata*).

- *clusterid*  
An array with two columns, while the number of rows is equal to the number of genes or the number of microarrays depending on whether genes or microarrays are being clustered. Each row contains the *x* and *y* coordinates of the cell in the rectangular SOM grid to which the gene or microarray was assigned.
- *celldata*  
An array with dimensions (*nxgrid*, *nygrid*, *number of microarrays*) if genes are being clustered, or (*nxgrid*, *nygrid*, *number of genes*) if microarrays are being clustered. Each element [*ix*][*iy*] of this array is a 1D vector containing the gene expression data for the centroid of the cluster in the grid cell with coordinates (*ix*,*iy*).

## 9.4 Finding the cluster centroids: `clustercentroid`

```
cdata, cmask = clustercentroid(data, mask=None, clusterid=None, method='a',
transpose=0)
```

calculates the cluster centroids.

### Arguments

- *data*  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- *mask*  
Array of integers showing which data are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. If `mask==None`, then there are no missing data.
- *clusterid*  
Vector of integers showing to which cluster each element belongs. If *clusterid* is not given, then all elements are assumed to belong to the same cluster.
- *method*  
Specifies whether the arithmetic mean (`method=='a'`) or the median (`method=='m'`) is used to calculate the cluster center.
- *transpose*  
Determines if gene or microarray clusters are being considered. If `transpose==0`, then we are considering clusters of genes (rows). If `transpose==1`, then we are considering clusters of microarrays (columns).

## Return values

This function returns the tuple (*cdata*, *cmask*).

- *cdata*  
A 2D array containing the centroid data. The dimensions of this array are (*number of clusters*, *number of microarrays*) if genes were clustered, or (*number of genes*, *number of clusters*) if microarrays were clustered. Each row (if genes were clustered) or

column (if microarrays were clustered) contains the averaged gene expression data for corresponding to the centroid of one cluster that was found.

- *cmask*

This matrix stores which values in *cdata* are missing. If *cmask*[*i*][*j*]==0, then *cdata*[*i*][*j*] is missing. The dimensions of this array are (*number of clusters*, *number of microarrays*) if genes were clustered, or (*number of genes*, *number of clusters*) if microarrays were clustered.

## 9.5 The distance between two clusters: clusterdistance

`clusterdistance(data, mask=None, weight=None, index1=[0], index2=[0], dist='e', method='a', transpose=0)`  
calculates the distance between two clusters.

### Arguments

- **data**  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
Array of integers showing which data are missing. If *mask*[*i*][*j*]==0, then *data*[*i*][*j*] is missing. If *mask*==None, then there are no missing data.
- **weight**  
contains the weights to be used when calculating distances. If *weight*==None, then equal weights are assumed.
- **index1**  
contains the indices of the elements belonging to the first cluster.
- **index2**  
contains the indices of the elements belonging to the second cluster.
- **dist**  
defines the distance function to be used:
  - dist*=='c': correlation;
  - dist*=='a': absolute value of the correlation;
  - dist*=='u': uncentered correlation;
  - dist*=='x': absolute uncentered correlation;
  - dist*=='s': Spearman's rank correlation;
  - dist*=='k': Kendall's  $\tau$ ;
  - dist*=='e': Euclidean distance;
  - dist*=='h': Harmonically summed Euclidean distance;
  - dist*=='b': City-block distance.
- **method**  
Specifies how the distance between clusters is defined:
  - method*=='a': Distance between the two cluster centroids (arithmetic mean);

`method=='m'`: Distance between the two cluster centroids (median);  
`method=='s'`: Shortest pairwise distance between elements in the two clusters;  
`method=='x'`: Longest pairwise distance between elements in the two clusters;  
`method=='v'`: Average over the pairwise distances between elements in the two clusters.

- **transpose**  
Determines if gene or microarray clusters are being considered. If `transpose==0`, then we are considering clusters of genes (rows). If `transpose==1`, then we are considering clusters of microarrays (columns).

## Return values

This function returns the distance between the two clusters.

## 9.6 Calculating the distance matrix: `distancematrix`

`matrix = distancematrix(data, mask=None, weight=None, transpose=0, dist='e')`  
 returns the distance matrix between gene expression data.

## Arguments

- **data**  
Array containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
Array of integers showing which data are missing. If `mask[i][j]==0`, then `data[i][j]` is missing. If `mask==None`, then there are no missing data.
- **weight**  
contains the weights to be used when calculating distances. If `weight==None`, then equal weights are assumed.
- **transpose**  
Determines if genes or microarrays are being clustered. If `transpose==0`, genes (rows) are being clustered. If `transpose==1`, microarrays (columns) are clustered.
- **dist**  
defines the distance function to be used:
  - `dist=='c'`: correlation;
  - `dist=='a'`: absolute value of the correlation;
  - `dist=='u'`: uncentered correlation;
  - `dist=='x'`: absolute uncentered correlation;
  - `dist=='s'`: Spearman's rank correlation;
  - `dist=='k'`: Kendall's  $\tau$ ;
  - `dist=='e'`: Euclidean distance;
  - `dist=='h'`: Harmonically summed Euclidean distance;
  - `dist=='b'`: City-block distance.



## Return values

- *matrix* is a list of 1D arrays containing the distance matrix between the gene expression data. The number of columns in each row is equal to the row number. Hence, the first row has zero elements. An example of the return value is

```
matrix = [array([]),
          array([1.]),
          array([7., 3.]),
          array([4., 2., 6.])]
```

This corresponds to the distance matrix

$$\begin{pmatrix} 0 & 1 & 7 & 4 \\ 1 & 0 & 3 & 2 \\ 7 & 3 & 0 & 6 \\ 4 & 2 & 6 & 0 \end{pmatrix}$$

## 9.7 Handling Cluster/TreeView-type files

Cluster/TreeView are GUI-based codes for clustering gene expression data. They were originally written by Michael Eisen (<http://rana.lbl.gov>) while at Stanford University. Pycluster contains routines for reading and writing data files that correspond to the format specified for Cluster/TreeView. Particularly, by saving a clustering result in the TreeView format, that program can be used to visualize the clustering results. We recommend using Alok Saldanha's Java TreeView program (<http://genome-www.stanford.edu/~alok/TreeView>), which can display hierarchical as well as *k*-means clustering results.

### 9.7.1 Reading a data file: readdatafile

```
(data, mask, geneid, genename, gweight, gorder, expid, eweight, eorder,
uniqid) = readdatafile(filename)
```

reads a tab-delimited text file *filename* containing gene expression data in the format specified for Michael Eisen's Cluster/TreeView program. For a description of this file format, see the manual to Cluster/TreeView. It is available at Michael Eisen's lab website (<http://rana.lbl.gov/manuals/ClusterTreeView.pdf>) and at our website (<http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster/cluster3.pdf>).

This function returns the tuple (data, mask, geneid, genename, gweight, gorder, expid, eweight, eorder, uniqid).

## Return values

- **data**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise.
- **mask**  
This array shows which elements in the **data** array, if any, are missing. If **mask[i,j]==0**, then **data[i,j]** is missing.

- **geneid**  
This is a list containing a unique identifier for each genes (i.e., ORF numbers).
- **genename**  
This is a list containing a description for each gene (i.e., gene name).
- **gweight**  
The weights that are to be used to calculate the distance in expression profile between genes.
- **gorder**  
The preferred order in which genes should be stored in an output file.
- **expid**  
This is a list containing a description of each microarray, e.g. experimental condition.
- **eweight**  
The weights that are to be used to calculate the distance in expression profile between microarrays.
- **eorder**  
The preferred order in which microarrays should be stored in an output file.
- **uniqid**  
The string that was used instead of UNIQID in the data file.

Note that **genename**, **gweight**, **gorder**, **eweight**, and **eorder** are not necessarily present in the data file. If they are not present, their return value is **None**. Furthermore, if there are no missing values ( $\text{mask}[i,j] == 1$  for all  $i, j$ ), then **mask** is return as **None**.

### 9.7.2 Saving the clustering result: writeclusterfiles

`writeclusterfiles(jobname, data, geneid, expid, mask=None, geneclusters=None, genelinkdist=None, expclusters=None, explinkdist=None, genename=None, gweight=None, eweight=None, uniqid=None)`  
writes the text file *jobname.cdt*, *jobname.gtr*, *jobname.atr*, *jobname.kgg*, and/or *jobname.kag* for subsequent reading by the Java TreeView program.

#### Arguments

- **jobname**  
The string **jobname** is used as the base name for names of the files that are to be saved.
- **data**  
The data array containing the gene expression data. Genes are stored row-wise, while microarrays are stored column-wise.
- **mask**  
This array shows which elements in the **data** array, if any, are missing. If  $\text{mask}[i,j] == 0$ , then  $\text{data}[i,j]$  is missing.
- **geneid**  
This is a list containing a unique identifier for each genes (i.e., ORF numbers).
- **expid**  
This is a list containing a description of each microarray, e.g. experimental condition.

- **geneclusters**  
This is array describing the gene clustering result. In case of  $k$ -means clustering, this is a 1D array containing the number of the cluster each gene belongs to. It can be calculated using **kcluster**. In case of hierarchical clustering, **geneclusters** is an array with  $ngenes-1$  rows and two columns that describes the hierarchical clustering result. Each row corresponds to a node; the entries in the two columns refer to the two subnodes that were clustered. Genes are numbered from 0 to  $(ngenes-1)$ ; nodes are numbered from -1 to  $-(ngenes-1)$ .
- **genelinkdist**  
This is a vector with  $ngenes-1$  elements, describing the distance between the two subnodes for each node in the hierarchical clustering of genes. For  $k$ -means clustering results, **genelinkdist** is not needed.
- **expclusters**  
This is array describing the clustering result of experimental conditions. In case of  $k$ -means clustering, this is a 1D array containing the number of the cluster each experimental condition belongs to. It can be calculated using **kcluster**. In case of hierarchical clustering, **expclusters** is an array with  $nexps-1$  rows and two columns that describes the hierarchical clustering result. Each row corresponds to a node; the entries in the two columns refer to the two subnodes that were clustered. Experimental conditions are numbered from 0 to  $(nexps-1)$ ; nodes are numbered from -1 to  $-(nexps-1)$ .
- **explinkdist**  
This is a vector with  $nexps-1$  elements, describing the distance between the two subnodes for each node in the hierarchical clustering of experimental conditions. For  $k$ -means clustering results, **explinkdist** is not needed.
- **genename**  
This is a list containing a description for each gene (i.e., gene name). If **genename** is not given, then **genename** defaults to **geneid**.
- **gweight**  
The weights that are to be used to calculate the distance in expression profile between genes.
- **gorder**  
The preferred order in which genes should be stored in an output file.
- **eweight**  
The weights that are to be used to calculate the distance in expression profile between microarrays.
- **eorder**  
The preferred order in which microarrays should be stored in an output file.
- **uniqid**  
The string that was used instead of UNIQID in the data file. If **uniqid** is not given, then it defaults to "UNIQID".

### 9.7.3 Example calculation

This is an example of a hierarchical clustering calculation, using single linkage clustering for genes and maximum linkage clustering for experimental conditions. As the Euclidean dis-

tance is being used for gene clustering, it is necessary to scale the distances in `genelinkdist` such that they are all between zero and two. This is needed for the Java TreeView code to display the tree diagram. To cluster the experimental conditions, the uncentered correlation is being used. Consequently, the distances in `explinkdist` are already between zero and two. The example data `cyano.txt` can be found in the `data` subdirectory.

```
>>> from Pycluster import *
>>> (data, mask, geneid, genename, gweight, gorder, expid, eweight, eorder,
unqid) = readdatafile("cyano.txt")
>>> geneclusters, genelinkdist = treecluster(data, applyscale=1, method='s')
>>> expclusters, explinkdist = treecluster(data, dist='u', transpose=1)
>>> writeclusterfiles("cyano", data, geneid, expid, geneclusters =
geneclusters, genelinkdist = genelinkdist, expclusters = expclusters,
explinkdist = explinkdist)
```

For  $k$ -means clustering, we only need to pass the `geneclusters` and/or the `expclusters` arguments. As there is no `genelinkdist` or `explinkdist` argument, no scaling is needed.

```
>>> from Pycluster import *
>>> (data, mask, geneid, genename, gweight, gorder, expid, eweight, eorder,
unqid) = readdatafile("cyano.txt")
>>> (geneclusters, genecentroids, error, ifound) = kcluster(data, nclusters=5,
npass=1000)
>>> (expclusters, expcentroids, error, ifound) = kcluster(data, nclusters=2,
npass=100, transpose=1)
>>> writeclusterfiles("cyano", data, geneid, expid, geneclusters =
geneclusters, expclusters = expclusters)
```

## 9.8 Auxiliary routines

`median(data)`

returns the median of the 1D array `data`.

`mean(data)`

returns the mean of the 1D array `data`.

## 10 Using the C Clustering Library with Perl: Algorithm::Cluster

Algorithm::Cluster is a Perl wrapper extension of the C Clustering Library written by John Nolan of the University of California, Santa Cruz.

Algorithm::Cluster requires Perl 5.6.0 at a minimum. It will not compile properly with 5.005\_03 or previous versions of Perl. It has been tested on Win32, Mac OS X, Linux, OpenBSD and Solaris.

To install Algorithm::Cluster on a UNIX or Linux machine, you can download the source bundle from the main site hosting Algorithm::Cluster. You will need an ANSI C compiler; GNU's free gcc compiler will do. Unpack the distribution and type the following familiar commands to compile, test and install the module:

```
perl Makefile.PL
make
make test
make install
```

You can also use the CPAN shell from within Perl to download the module and install it.

If you use ActiveState Perl on Windows, use the Perl Package Manager ppm to install Algorithm::Cluster by executing the following command from the DOS command prompt.

```
ppm install http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster/Algorithm-Cluster.ppd
```

Algorithm::Cluster offers the following functions:

- kcluster
- treecluster
- somcluster
- clusterdistance
- mean
- median

A later version of the module will include the functions `clustercentroid`, `readdatafile` and `writedatafile`.

### 10.1 Using named parameters

Most of the interface functions in Algorithm::Cluster expect named parameters. This is implemented by passing a hash as a parameter to the function. For example, if a Perl function `sign_up()` accepts three named parameters, `name`, `program` and `class`, then you can invoke the function like this:

```
$return_value = sign_up(
    'name' => 'Mr. Smith',
    'program' => 'Biology',
    'class' => 'Intro to Molecular Biology',
);
```

When the function parses its parameters, it will create a hash, on the fly, with three keys. The function can access the values by referring to the hash.

This is convenient for several reasons. First, it means that you can pass the parameters in any order. Both invocations below are valid:

```
$return_value = sign_up(
    'class' => 'Intro to Molecular Biology',
    'name' => 'Ms. Jones',
    'program' => 'Biology',
);
$return_value = sign_up(
    'name' => 'Miss Chen',
    'program' => 'Biology',
    'class' => 'Intro to Molecular Biology',
);
```

If the function defines default values for parameters, you can also leave some parameters out, and the function will still know which parameter is which:

```
$return_value = sign_up(
    'name' => 'Ms. Jones',
);
```

You can define the hash on your own, and pass this to the function. This is useful if your function accepts a long list of parameters, and you intend to call it several times, (mostly) reusing the same values. You can implement your own defaults:

```
%student = (
    'name' => 'Mr. Smith',
    'program' => 'Biology',
    'class' => 'Intro to Molecular Biology',
);
$return_value = sign_up(%student);

$hash{student} = 'Ms. Jones';
$return_value = sign_up(%student);

$hash{student} = 'Miss Chen';
$return_value = sign_up(%student);
```

## 10.2 References to arrays, and two-dimensional matrices

Perl implements two-dimensional matrices using references. For example, a reference to a one-dimensional array (a row) can be defined like this:

```
$row = [ 1, 2 ];
```

In this example, `$row` itself is not an array, but a reference to the array (1, 2). (The square brackets indicate that we want to create a reference.) `$row->[0]` equals 1 and `$row->[1]` equals 2. A  $3 \times 2$  matrix of integers can be defined like this:

```
$row0 = [ 1, 2 ];
$row1 = [ 3, 4 ];
$row2 = [ 5, 6 ];
$data = [ $row0, $row1, $row2 ];
```

Or, more succinctly:

```
$data = [
    [ 1, 2 ],
    [ 3, 4 ],
    [ 5, 6 ],
];
```

In this example, `$data->[0]->[1]` equals 2, while `$data->[2]->[0]` equals 5.

Many of the functions available in Algorithm::Cluster expect data to be in the form of a two dimensional array, like the example above. Some functions also return references to data structures like this.

### 10.3 The *k*-means clustering algorithm: kcluster

The function `kcluster()` implements the *k*-means clustering algorithm. In the example invocation below, we have created `$param{data}` as an empty matrix, because that is the default value, but you must populate `$param{data}` with real data, in order to invoke `kcluster()` properly.

```
my %param = (
    nclusters => 3,
    data => [[]],
    mask => '',
    weight => '',
    transpose => 0,
    npass => 10,
    method => 'a',
    dist => 'e',
);
my ($clusters, $centroids, $found) = kcluster(%param);
```

#### Arguments

- **data**  
A reference to a two-dimensional matrix containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.

- **nclusters**  
The number of clusters  $k$ .
- **mask**  
A reference to a two-dimensional matrix of integers showing which data are missing. If `$param{mask}->[i]->[j]==0`, then `$param{data}->[i]->[j]` is missing. If `mask` is `''` (i.e., the null string, and not a reference at all), then there are no missing data.
- **weight**  
A reference to an array containing the weights to be used when calculating distances. If `weight` equals `''` (i.e., the null string, and not a reference at all), then equal weights are assumed. If `transpose==0`, the length of this array must equal the number of columns in the data matrix. If `transpose==1`, the length of the `weight` array should equal the number of rows in the data matrix. If `weight` has a different length, the entire array will be ignored.
- **transpose**  
Determines if genes or microarrays are being clustered. If `$param{transpose}==0`, genes (rows) are being clustered. If `$param{transpose}==1`, microarrays (columns) are clustered.
- **npass**  
The number of times the  $k$ -means clustering algorithm is performed, each time with a different (random) initial condition.
- **method**  
A one-character flag, indicating how the center of a cluster is found:
  - 'a': arithmetic mean
  - 'm': median

For any other values of `method`, the arithmetic mean is used.
- **dist**  
A one-character flag, defining the distance function to be used:
  - 'c': correlation
  - 'a': absolute value of the correlation
  - 'u': uncentered correlation
  - 'x': absolute uncentered correlation
  - 's': Spearman's rank correlation
  - 'k': Kendall's  $\tau$ ;
  - 'e': Euclidean distance
  - 'h': Harmonically summed Euclidean distance
  - 'b': City-block distance

For other values of `dist`, the default (Euclidean distance) is used.

This function returns a list of three items: `$clusterid`, `$centroids`, `$nfound`.

- **\$clusterid**  
`$clusterid` is a reference to an array whose length is equal to the number of rows in the data array. Each element in the `clusterid` array contains the number of the cluster to which each gene/microarray was assigned.



- **\$centroids**  
**\$centroids** is a reference to a two-dimensional matrix containing the coordinates of each cluster's centroid. The dimensions of this matrix depend on the value of the **transpose** parameter. If **transpose** is zero, then the dimensions will be the number of clusters (passed in via the **nclusters** parameter) by the number of columns in the data matrix. If **transpose** is 1, then the dimensions will be the number of rows in the data matrix by the number of clusters.
- **\$nfound**  
**\$nfound** is the number of times the optimal solution was found.

## 10.4 Hierarchical clustering: treecluster

The pairwise single-, maximum-, average-, and centroid-linkage clustering methods are accessible through the function **treecluster**.

```
my %param = (
    data => [[]],
    mask => '',
    weight => '',
    applyscale => 0,
    transpose => 0,
    dist => 'e',
    method => 's',
);

my ($result, $linkdist) = Algorithm::Cluster::treecluster(%param);
```

### Arguments

- **data**  
A reference to a two-dimensional matrix containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
A reference to a two-dimensional matrix of integers showing which data are missing. If **\$param{mask}->[i]->[j]==0**, then **\$param{data}->[i]->[j]** is missing. If **mask** is **''** (i.e., the null string, and not a reference at all), then there are no missing data.
- **weight**  
A reference to an array containing the weights to be used when calculating distances. If **weight** equals **''** (i.e., the null string, and not a reference at all), then equal weights are assumed. If **transpose==0**, the length of this array must equal the number of columns in the data matrix. If **transpose==1**, the length of the **weight** array should equal the number of rows in the data matrix. If **weight** has a different length, the entire array will be ignored.
- **applyscale**  
If **applyscale** is nonzero, then the distances in **linkdist** are scaled such that all distances are between zero and two, as in case of the Pearson distance. Otherwise, no scaling is applied.

- **transpose**  
Determines if genes or microarrays are being clustered. If `$param{transpose}==0`, genes (rows) are being clustered. If `$param{transpose}==1`, microarrays (columns) are clustered.
- **dist**  
A one-character flag, defining the distance function to be used:
  - 'c': correlation
  - 'a': absolute value of the correlation
  - 'u': uncentered correlation
  - 'x': absolute uncentered correlation
  - 's': Spearman's rank correlation
  - 'k': Kendall's tau
  - 'e': Euclidean distance
  - 'h': Harmonically summed Euclidean distance
  - 'b': City-block distance

This function returns a list of two items: `$result`, `$linkdist`.

- **\$result**  
`$result` is a reference to a two-dimensional matrix. If `$param{transpose}==0`, then the number of rows in `$result` equals one less than the number of rows (genes) in the original data array; if `$param{transpose}==1`, then the number of rows in `$result` equals one less than the number of columns (microarrays) in the original data array. Each row in this matrix describes a pairwise linkage event between two items, either rows and clusters of rows (if rows/genes were clustered), or columns and clusters of columns (if columns/microarrays were clustered). Rows or columns are numbered from 0 to (number of items -1), while clusters are numbered -1 to -(number of items-1).
- **\$linkdist**  
`$linkdist` is a reference to an array, whose length is equal to the number of rows in the `$result` matrix. For each node, the array element contains the distance between the two subnodes that were joined.

## 10.5 Self-Organizing Maps: somcluster

The `somcluster()` function implements a Self-Organizing Map on a rectangular grid.

```
my %param = (
    data => [[]],
    mask => '',
    weight => '',
    transpose => 0,
    nxgrid => 10,
    nygrid => 10,
    niter => 100,
    dist => 'e',
);
my ($clusterid) = Algorithm::Cluster::somcluster(%param);
```

## Arguments

- **data**  
A reference to a two-dimensional matrix containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
A reference to a two-dimensional matrix of integers showing which data are missing. If `$param{mask}>[i]>[j]==0`, then `$param{data}->[i]->[j]` is missing. If `mask` is `''` (i.e., the null string, and not a reference at all), then there are no missing data.
- **weight**  
A reference to an array containing the weights to be used when calculating distances. If `weight` equals `''` (i.e., the null string, and not a reference at all), then equal weights are assumed. If `transpose==0`, the length of this array must equal the number of columns in the data matrix. If `transpose==1`, the length of the `weight` array should equal the number of rows in the data matrix. If `weight` has a different length, the entire array will be ignored.
- **transpose**  
Determines if genes or microarrays are being clustered. If `$param{transpose}==0`, genes (rows) are being clustered. If `$param{transpose}==1`, microarrays (columns) are clustered.
- **nxgrid, nygrid**  
Both parameters are integers, indicating the number of cells horizontally and vertically in the rectangular grid, on which the Self-Organizing Map is calculated.
- **inittau**  
The initial value for the neighborhood function, as given by the parameter  $\tau$ . The default value for `inittau` is 0.02, which was used in Michael Eisen's Cluster/TreeView program.
- **niter**  
The number of iterations to be performed.
- **dist**  
A one-character flag, defining the distance function to be used:
  - 'c': correlation
  - 'a': absolute value of the correlation
  - 'u': uncentered correlation
  - 'x': absolute uncentered correlation
  - 's': Spearman's rank correlation
  - 'k': Kendall's tau
  - 'e': Euclidean distance
  - 'h': Harmonically summed Euclidean distance
  - 'b': City-block distance

This function returns one value, `$clusterid`, which is a reference to a two-dimensional matrix. If `$param{transpose}==0`, then the number of rows in `$clusterid` equals the number of rows (genes) in the original data array; if `$param{transpose}==1`, then then the

number of rows in `$clusterid` equals the number of columns (microarrays) in the original data array. Each row in the array `clusterid` contains the x and y coordinates of the cell in the rectangular SOM grid to which the gene or microarray was assigned.

## 10.6 The distance between two clusters: `clusterdistance`

The `clusterdistance` routine calculates the distance between two clusters.

```
my %param = (
    data => [],
    mask => '',
    weight => '',
    cluster1 => [],
    cluster2 => [],
    dist => 'e',
    method => 'a',
    transpose => 0,
);

my ($distance) = Algorithm::Cluster::clusterdistance(%param);
```

### Arguments

- **data**  
A reference to a two-dimensional matrix containing the gene expression data, where genes are stored row-wise and microarray experiments column-wise.
- **mask**  
A reference to a two-dimensional matrix of integers showing which data are missing. If `$param{mask}>[i]>[j]==0`, then `$param{data}->[i]->[j]` is missing. If `mask` is `''` (i.e., the null string, and not a reference at all), then there are no missing data.
- **weight**  
A reference to an array containing the weights to be used when calculating distances. If `weight` equals `''` (i.e., the null string, and not a reference at all), then equal weights are assumed. If `transpose==0`, the length of this array must equal the number of columns in the data matrix. If `transpose==1`, the length of the `weight` array should equal the number of rows in the data matrix. If `weight` has a different length, the entire array will be ignored.
- **cluster1**  
contains the indices of the elements belonging to the first cluster.
- **cluster2**  
contains the indices of the elements belonging to the second cluster.
- **dist**  
A one-character flag, defining the distance function to be used:
  - 'c': correlation
  - 'a': absolute value of the correlation
  - 'u': uncentered correlation

- 'x': absolute uncentered correlation
- 's': Spearman's rank correlation
- 'k': Kendall's tau
- 'e': Euclidean distance
- 'h': Harmonically summed Euclidean distance
- 'b': City-block distance

- **method**

A one-character flag, indicating how the center of a cluster is found:

- 'a': Distance between the two cluster centroids (arithmetic mean)
- 'm': Distance between the two cluster centroids (median)
- 's': Shortest distance between elements in the two clusters
- 'x': Longest pairwise distance between elements in the two clusters
- 'v': Average over the pairwise distances between elements in the two clusters.

For any other values of **method**, the arithmetic mean is used.

- **transpose**

Determines if genes or microarrays are being clustered. If `$param{transpose}==0`, genes (rows) are being clustered. If `$param{transpose}==1`, microarrays (columns) are clustered.

## 10.7 Auxiliary routines

**median(\$data)**

Returns the median of the data. `$data` is a reference to a (one-dimensional) array of numbers.

**mean(\$data)**

Returns the mean of the data. `$data` is a reference to a (one-dimensional) array of numbers.

## 11 Compiling and linking

In the instructions below, *<version>* refers to the version number. The C Clustering Library complies with the ANSI-C standard since version 1.04. As of version 1.06, the C Clustering Library makes use of `autoconf/automake` to make the installation process easier. To install the library for use with Python, use the `setup.py` script instead, as described below.

### 11.1 Installing the C Clustering Library for Python

Pycluster is available as part of the Biopython distribution and as a separate package. To install Pycluster as a separate package, download `Pycluster-<version>.tar.gz` from <http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>. Unpack this file:

```
gunzip Pycluster-<version>.tar.gz
```

```
tar -xvf Pycluster-<version>.tar
```

and change to the directory `Pycluster-<version>`. Type

```
python setup.py install
```

from this directory. This will compile the library and install it for use with Python. If the installation was successful, you can remove the directory `Pycluster-<version>`. For Python on Windows (run from a DOS command window, or with a graphical user interface such as IDLE, PyCrust, PyShell, or PythonWin), a binary installer is available from <http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>.

Installation instructions for Biopython are available from the Biopython website (<http://www.biopython.org>).

If you want to add Python bindings for other functions in the C Clustering Library, or if you want to add more functions, you can use Pyfort to generate the C extension module automatically. Pyfort can be downloaded from <http://pyfortran.sourceforge.net>.

### 11.2 Installing the C Clustering Library for Perl

Algorithm::Cluster, written by John Nolan of the University of California, Santa Cruz, is an extension to Perl that gives access to the routines in the C Clustering Library. To install Algorithm::Cluster, download `Algorithm-Cluster-<version>.tar.gz` from <http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster> or from CPAN. Next, unpack this file with

```
gunzip Algorithm-Cluster-<version>.tar.gz
```

```
tar -xvf Algorithm-Cluster-<version>.tar
```

and change to the directory `Algorithm-Cluster-<version>`. Type

```
perl Makefile.PL
```

which will create a Makefile. To compile and install, type

```
make
```

```
make install
```

from this directory. You can execute

```
make test
```

to run some scripts that test the Algorithm::Cluster module. Some example Perl scripts

can be found in the `perl/examples` subdirectory. If the installation was successful, you can remove the directory `Algorithm-Cluster-<version>`.

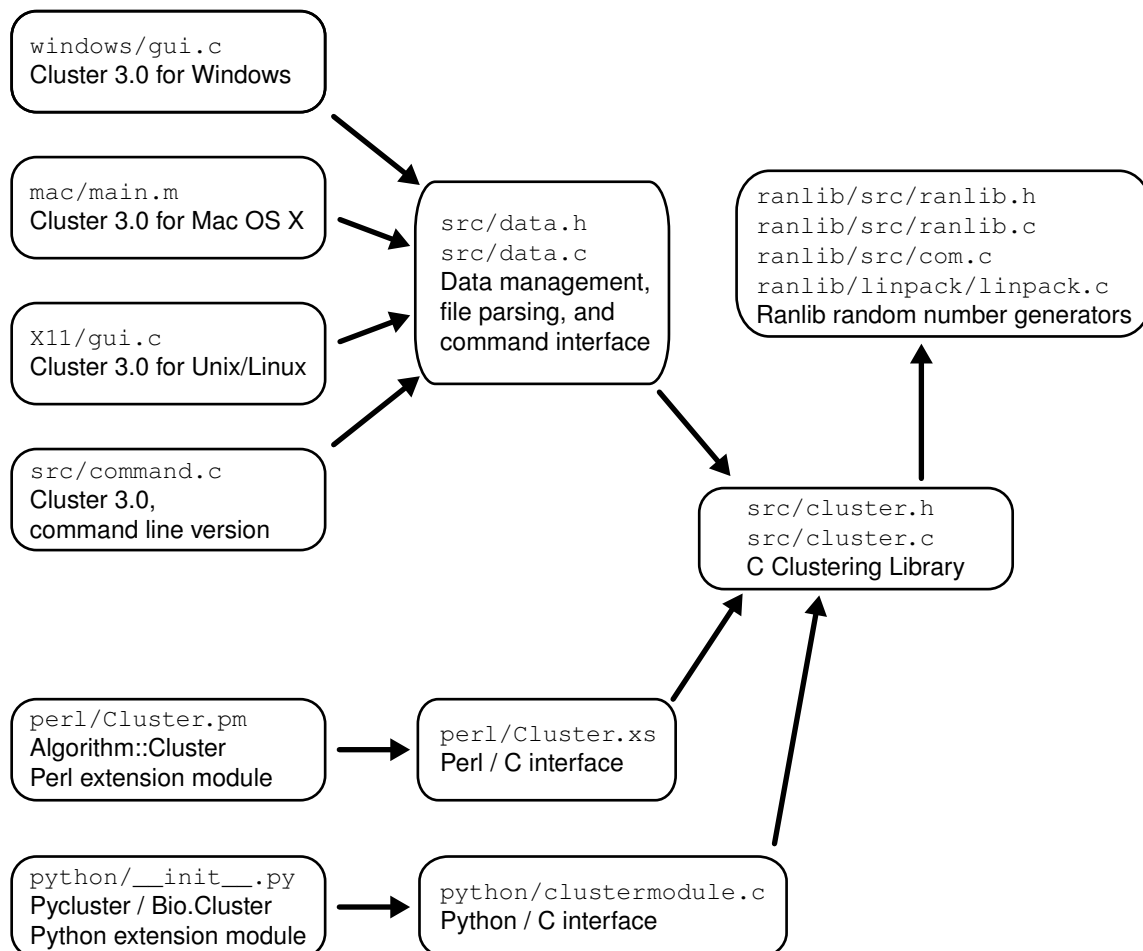
If you use ActiveState Perl on Windows, you can use the Perl Package Manager by executing

```
ppm install http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster/Algorithm-Cluster.ppd
```

from the DOS command prompt. This assumes that you are using Perl 5.8.0 from ActiveState.

### 11.3 Accessing the C Clustering Library from C/C++

To call the routines in the C Clustering Library from your own C or C++ program, simply collect the relevant source files and compile them together with your program. The figure below shows the dependency structure for the source files in the C Clustering Library.



To use the routines in the C Clustering Library, put `#include <cluster.h>` in your source code. If your program is written in C++, use

```
extern "C" {
#include <cluster.h>
}
```

instead. To compile a C or C++ program with the C Clustering Library, add the relevant source files to the compile command. For example, a C program `myprogram.c` can be compiled and linked by

```
gcc -o myprogram myprogram.c cluster.c ranlib.c com.c linpack.c
```

An example C program that makes use of the C Clustering Library can be found in the `example` subdirectory.

## 11.4 Installing Cluster 3.0 for Windows

The easiest way to install Cluster 3.0 for Windows is to use the Windows installer (<http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>). If you want to compile Cluster 3.0 from the source, change to the `windows` directory, and type `make`. This will compile the C Clustering Library, the Cluster 3.0 GUI, the Windows help files and the documentation. To compile the GUI, you need an ANSI C compiler such as GNU `gcc`. To compile the resources needed for the GUI, you will need the GNU program `windres`. To generate the help files, you need the HTML Help SDK, which can be downloaded from Microsoft. You will also need GNU `makeinfo`.

To generate the Windows installer, type  
`make clustersetup.exe`

For this, you will need the Inno Setup Compiler, which can be downloaded from <http://www.jrsoftware.org>.

## 11.5 Installing Cluster 3.0 for Mac OS X

Cluster 3.0 for Mac OS X can be installed most easily by using the prebuilt package that is available at <http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>. If you want to recompile Cluster 3.0, it is easiest to use the Project Builder and Interface Builder that are part of Mac OS X. The directory `mac` contains the project file that was used.

## 11.6 Installing Cluster 3.0 for Linux/Unix

Cluster 3.0 was ported to Linux/Unix using the Motif libraries. Motif is installed on most Linux/Unix computers. You will need a version compliant with Motif 2.1, such as Open Motif (<http://www.opengroup.org>), which is available at <http://www.motifzone.net>. Currently, LessTif (<http://www.lesstif.org>) does not work correctly with Cluster 3.0.

To install Cluster 3.0 on Linux/Unix, type  
`./configure --with-motif`  
`make`  
`make install`

This will create the executable `cluster` and install it in `/usr/local/bin`. Some auxiliary files will be installed in `/usr/local/cluster`.



## 11.7 Installing Cluster 3.0 as a command line program

Cluster 3.0 can also be installed as a command line program, in which the action taken by the program depends on the command line parameters. To install Cluster 3.0 as a command line program, download the source code for the C Clustering Library from our website <http://bonsai.ims.u-tokyo.ac.jp/~mdehoon/software/cluster>. Unpack and untar the file, and change to the directory `cluster-<version>`. Then type

```
./configure
```

```
make
```

```
make install
```

For the last step, you may need superuser privileges. For more information about the command line options, check the Cluster 3.0 manual.

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